FACULTY OF ECONOMICS AND BUSINESS
UNIVERSITAS INDONESIA

Final Exam First Semester of 2018/2019
Statistics for Economics and Business

Date : December 18th, 2018
Time : 150 minutes
Lecturers : Team

You may use a calculator.
The use of celluler phone during the exam is strictly prohibited.

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1. **(25 points)** With the growing life style of people drinking coffee, it is found that in recent years about two-thirds of Indonesian households purchased ground coffee. It is known that the monthly expenditure for household purchasing ground coffee is normally distributed with a mean of Rp65,000.00 and a standard deviation of Rp10,000.00.
   a. Explain the characteristics of the normal distribution! (5 points)
   b. Find the probability that a household spends less than Rp 35,000.00 (5 points)
   c. 99% of the households spend less than what amount? (7 points)
   d. What is the lower and upper limits of the interval that contains 95% of the monthly expenditures that are in the middle of the distribution of expenditures for ground coffee? (8 points)

2. **(20 points)** Birth weight in a country follows a normal distribution with a mean of 2,850 grams and a standard deviation of 550 grams.
   a. Explain the attributes of sampling distribution of the sample mean based on a random draw of 20 infants. (5 points)
   b. Find the probability that the mean weight of 20 randomly selected infants is below 2,500 grams. (5 points)
   c. Find the probability that the mean weight of 20 randomly selected infants is between 2,500 grams and 3,000 grams. (5 points)
   d. What is the probability that the mean weight of 20 randomly selected infants above 3,000 grams? (5 points)

3. **(30 points) The** ABC Elementary School has 1,000 students. The principal of the school believes that the average IQ of students at ABC is at least 110. To prove her point, she administers an IQ test to 20 randomly selected students. Among the sampled students, the average IQ is 108 with a standard deviation of 10. Based on these results, should the principal accept or reject her original hypothesis? Assume a significance level of 0.01. (Assume that test scores in the population are normally distributed)

   a. Specify the null and the alternative hypotheses for the test (5 points)
   b. Given the significance level, find the critical value. (5 points)
   c. Calculate the value of the test statistic. (7 points)
   d. State the conclusion and interpret the results? (5 points)

e. If, in fact the mean is 112 and standard deviation is 10.9, what will the probability of Type 2 error of our test be? (8 points)

4. **(25 points)** Assume now is 2022. In 2020 'Berita Sepuluh' sought information on how young Indonesian adults viewed their parents' marriage. In a telephone poll, one of the questions they asked of six hundred and two (602) 18–29 years old Indonesians was "Would you like to have a marriage like the one your parents have?" Forty-four percent (44%) responded "Yes." 'Berita Sepuluh' was interested in determining the percentage of the 18–29 years old Indonesians who would answer "Yes" to this question.

   Which one of the following statements is false? Give a clear and short **argument**. You might also need to **prove** your answer.

   a. The parameter to be estimated is population mean. [2 point]
   b. In this case, 0.44 is the parameter of population. [2 point]
   c. We need to use a finite population correction factor in order to estimate a confidence interval for this case. [2 point]
   d. In order to estimate a confidence interval, we need to use *t*-distribution because we don't know the population standard deviation. [2 point]
   e. A 95% confidence interval of the population parameter of interest is [0.400 and 0.500]. [5 point]
   f. If two thousand four hundred (2,400) 18-29 years old Indonesians had been sampled instead of six hundred and two (602) 18-29 years old Indonesians, then the new 95% confidence interval would be approximately half as wide. [6 point]
   g. In 2022, a new survey will be conducted. With 0.95 confidence level and margin of error as 0.06, determine the sample size needed for the study. [6 point]

Selected Formulas

$$s^2 = \frac{\sum (x_i - \bar{x})^2}{n-1} \; ; \; s^2 = \frac{\sum (m_i - \bar{x})^2 f_i}{n-1} \; ; \; \sigma^2 = \frac{\sum (x_i - \mu)^2}{N} \; ; \; \sigma^2 = \frac{\sum (m_i - \mu)^2 f_i}{N}$$

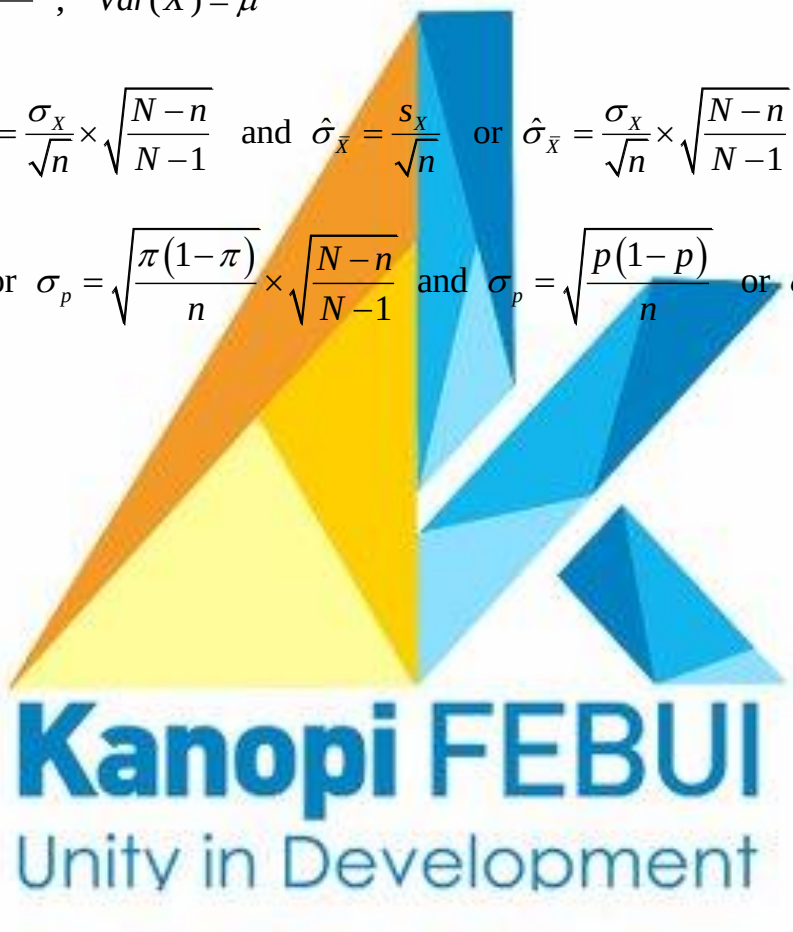
$$E(X) = \mu = \sum x_i P(X = x_i) \; ; \; Var(X) = \sigma^2 = \sum \left[(x_i - \mu)^2 P(X = x_i) \right]$$

$$P(X = x) = \binom{n}{x} \pi^x (1-\pi)^{n-x} \; ; \; E(X) = \mu_X = n\pi \; ; \; Var(X) = \sigma^2 = n\pi(1-\pi)$$

$$P(X = x) = \frac{e^{-\mu} \mu^x}{x!} \; ; \; Var(X) = \mu$$

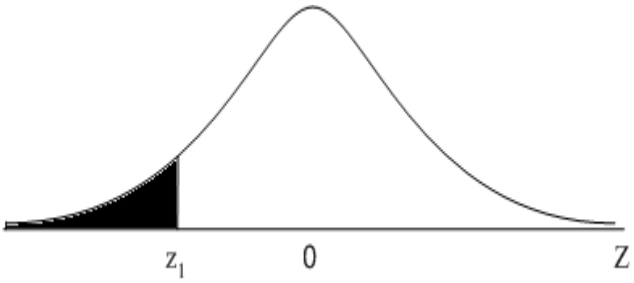
$$\sigma_{\bar{X}} = \frac{\sigma_X}{\sqrt{n}} \text{ or } \sigma_{\bar{X}} = \frac{\sigma_X}{\sqrt{n}} \times \sqrt{\frac{N-n}{N-1}} \text{ and } \hat{\sigma}_{\bar{X}} = \frac{s_X}{\sqrt{n}} \text{ or } \hat{\sigma}_{\bar{X}} = \frac{\sigma_X}{\sqrt{n}} \times \sqrt{\frac{N-n}{N-1}}$$

$$\sigma_p = \sqrt{\frac{\pi(1-\pi)}{n}} \text{ or } \sigma_p = \sqrt{\frac{\pi(1-\pi)}{n}} \times \sqrt{\frac{N-n}{N-1}} \text{ and } \sigma_p = \sqrt{\frac{p(1-p)}{n}} \text{ or } \sigma_p = \sqrt{\frac{p(1-p)}{n}} \times \sqrt{\frac{N-n}{N-1}}$$



Normal Standard Z Distribution:

Content of the table shows area under the curve orprobability of Z up to z_1 [$P(Z < z_1)$]



	0.00	*0.01*	*0.02*	*0.03*	*0.04*	*0.05*	*0.06*	*0.07*	*0.08*	*0.09*
–3.0	0.0013	0.0013	0.0013	0.0012	0.0012	0.0011	0.0011	0.0011	0.0010	0.0010
–2.9	0.0019	0.0018	0.0018	0.0017	0.0016	0.0016	0.0015	0.0015	0.0014	0.0014
–2.8	0.0026	0.0025	0.0024	0.0023	0.0023	0.0022	0.0021	0.0021	0.0020	0.0019
–2.7	0.0035	0.0034	0.0033	0.0032	0.0031	0.0030	0.0029	0.0028	0.0027	0.0026
–2.6	0.0047	0.0045	0.0044	0.0043	0.0041	0.0040	0.0039	0.0038	0.0037	0.0036
–2.5	0.0062	0.0060	0.0059	0.0057	0.0055	0.0054	0.0052	0.0051	0.0049	0.0048
–2.4	0.0082	0.0080	0.0078	0.0075	0.0073	0.0071	0.0069	0.0068	0.0066	0.0064
–2.3	0.0107	0.0104	0.0102	0.0099	0.0096	0.0094	0.0091	0.0089	0.0087	0.0084
–2.2	0.0139	0.0136	0.0132	0.0129	0.0125	0.0122	0.0119	0.0116	0.0113	0.0110
–2.1	0.0179	0.0174	0.0170	0.0166	0.0162	0.0158	0.0154	0.0150	0.0146	0.0143
–2.0	0.0228	0.0222	0.0217	0.0212	0.0207	0.0202	0.0197	0.0192	0.0188	0.0183
–1.9	0.0287	0.0281	0.0274	0.0268	0.0262	0.0256	0.0250	0.0244	0.0239	0.0233
–1.8	0.0359	0.0351	0.0344	0.0336	0.0329	0.0322	0.0314	0.0307	0.0301	0.0294
–1.7	0.0446	0.0436	0.0427	0.0418	0.0409	0.0401	0.0392	0.0384	0.0375	0.0367
–1.6	0.0548	0.0537	0.0526	0.0516	0.0505	0.0495	0.0485	0.0475	0.0465	0.0455
–1.5	0.0668	0.0655	0.0643	0.0630	0.0618	0.0606	0.0594	0.0582	0.0571	0.0559
–1.4	0.0808	0.0793	0.0778	0.0764	0.0749	0.0735	0.0721	0.0708	0.0694	0.0681
–1.3	0.0968	0.0951	0.0934	0.0918	0.0901	0.0885	0.0869	0.0853	0.0838	0.0823
–1.2	0.1151	0.1131	0.1112	0.1093	0.1075	0.1056	0.1038	0.1020	0.1003	0.0985
–1.1	0.1357	0.1335	0.1314	0.1292	0.1271	0.1251	0.1230	0.1210	0.1190	0.1170
–1.0	0.1587	0.1562	0.1539	0.1515	0.1492	0.1469	0.1446	0.1423	0.1401	0.1379
–0.9	0.1841	0.1814	0.1788	0.1762	0.1736	0.1711	0.1685	0.1660	0.1635	0.1611
–0.8	0.2119	0.2090	0.2061	0.2033	0.2005	0.1977	0.1949	0.1922	0.1894	0.1867
–0.7	0.2420	0.2389	0.2358	0.2327	0.2296	0.2266	0.2236	0.2206	0.2177	0.2148
–0.6	0.2743	0.2709	0.2676	0.2643	0.2611	0.2578	0.2546	0.2514	0.2483	0.2451
–0.5	0.3085	0.3050	0.3015	0.2981	0.2946	0.2912	0.2877	0.2843	0.2810	0.2776
–0.4	0.3446	0.3409	0.3372	0.3336	0.3300	0.3264	0.3228	0.3192	0.3156	0.3121
–0.3	0.3821	0.3783	0.3745	0.3707	0.3669	0.3632	0.3594	0.3557	0.3520	0.3483
–0.2	0.4207	0.4168	0.4129	0.4090	0.4052	0.4013	0.3974	0.3936	0.3897	0.3859
–0.1	0.4602	0.4562	0.4522	0.4483	0.4443	0.4404	0.4364	0.4325	0.4286	0.4247
–0.0	0.5000	0.4960	0.4920	0.4880	0.4840	0.4801	0.4761	0.4721	0.4681	0.4641

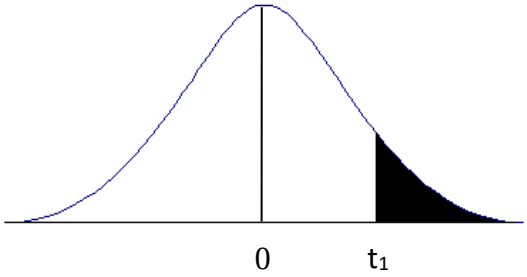
	0.00	***0.01***	***0.02***	***0.03***	***0.04***	***0.05***	***0.06***	***0.07***	***0.08***	***0.09***
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
3.0	0.9987	0.9987	0.9987	0.9988	0.9988	0.9989	0.9989	0.9989	0.9990	0.9990
3.1	0.9990	0.9991	0.9991	0.9991	0.9992	0.9992	0.9992	0.9992	0.9993	0.9993

Student *t* Distribution:

Content in the table shows that with the degrees of freedom on the left margin, the probability of the t-value will be greater than content in the table is α as showed at the top of the margin [$P(t > t_1) = \alpha$].

For df = 12, P (t >1.7823) = 0.05; and

For df = 12, P (t < – 1.7823) = 0.05



df \ α	0.1	0.05	0.025	0.01	0.005
1	3.0777	6.3137	12.7062	31.8210	63.6559
2	1.8856	2.9200	4.3027	6.9645	9.9250
3	1.6377	2.3534	3.1824	4.5407	5.8408
4	1.5332	2.1318	2.7765	3.7469	4.6041
5	1.4759	2.0150	2.5706	3.3649	4.0321
6	1.4398	1.9432	2.4469	3.1427	3.7074
7	1.4149	1.8946	2.3646	2.9979	3.4995
8	1.3968	1.8595	2.3060	2.8965	3.3554
9	1.3830	1.8331	2.2622	2.8214	3.2498
10	1.3722	1.8125	2.2281	2.7638	3.1693
11	1.3634	1.7959	2.2010	2.7181	3.1058
12	1.3562	1.7823	2.1788	2.6810	3.0545
13	1.3502	1.7709	2.1604	2.6503	3.0123
14	1.3450	1.7613	2.1448	2.6245	2.9768
15	1.3406	1.7531	2.1315	2.6025	2.9467
16	1.3368	1.7459	2.1199	2.5835	2.9208
17	1.3334	1.7396	2.1098	2.5669	2.8982
18	1.3304	1.7341	2.1009	2.5524	2.8784
19	1.3277	1.7291	2.0930	2.5395	2.8609
20	1.3253	1.7247	2.0860	2.5280	2.8453
21	1.3232	1.7207	2.0796	2.5176	2.8314
22	1.3212	1.7171	2.0739	2.5083	2.8188
23	1.3195	1.7139	2.0687	2.4999	2.8073
24	1.3178	1.7109	2.0639	2.4922	2.7970
25	1.3163	1.7081	2.0595	2.4851	2.7874
26	1.3150	1.7056	2.0555	2.4786	2.7787
27	1.3137	1.7033	2.0518	2.4727	2.7707
28	1.3125	1.7011	2.0484	2.4671	2.7633
29	1.3114	1.6991	2.0452	2.4620	2.7564
30	1.3104	1.6973	2.0423	2.4573	2.7500
40	1.3031	1.6839	2.0211	2.4233	2.7045
50	1.2987	1.6759	2.0086	2.4033	2.6778
80	1.2922	1.6641	1.9901	2.3739	2.6387
100	1.2901	1.6602	1.9840	2.3642	2.6259
120	1.2886	1.6576	1.9799	2.3578	2.6174